

FOREST MANAGEMENT FROM MULTICRITERIA AND GROUP DECISION MAKING VIEW – A METHODOLOGICAL CHALLENGE

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Presented at IUFRO 4.05.00 meeting in Darmstadt
October 28, 2009



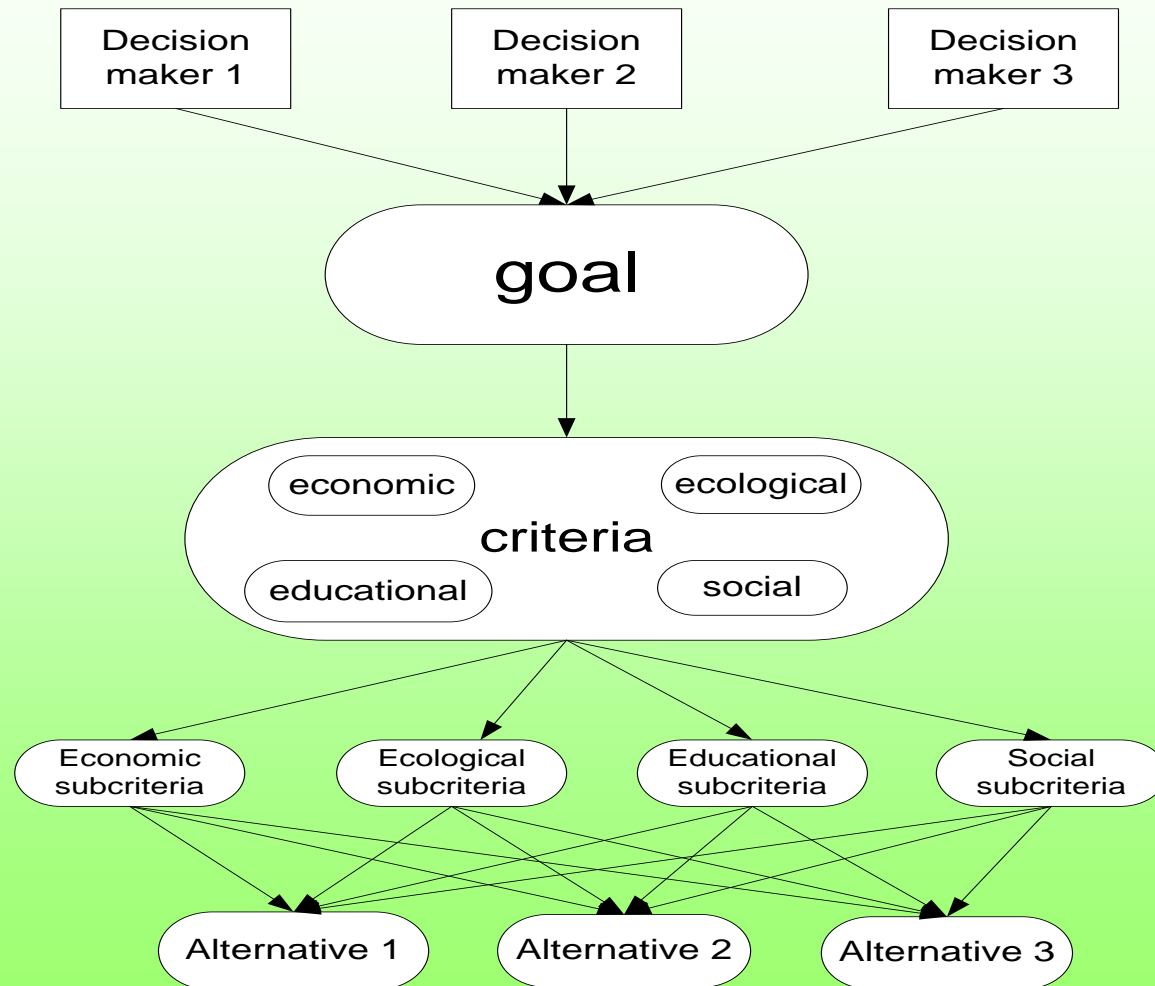
Framework

- For sustainable, multiple use and long term forest management **several alternatives** (scenarios, decisions) are developed
- Each scenario is affected by **several criteria**: economic, ecological, social, educational, etc.
- **Several decision makers** (different social groups) identify and assess the forest management alternatives

Decision making approach to forest management

- Forest management problem formulation
- Forest data and literature
- Defining the management goal
- Defining the forest management alternatives
- Deciding criteria and indicators (sub-criteria, attributes)
- Defining decision groups and their preferences for criteria and indicators
- Evaluating the criteria and indicators
- Weights assignment by the support of the appropriate methodological tool

Hierarchical structure of the problem



Forest management

- The **alternatives (decisions)** in forest management are **affected** by multiple criteria and several attributes (sub-criteria):

Criteria

Sub-criteria

Economic

timber production, hunting, increase of local income, job opportunities, sustainable economic development of the area, silvicultural treatments, taxes and other fixed costs, change of market prices

Ecological

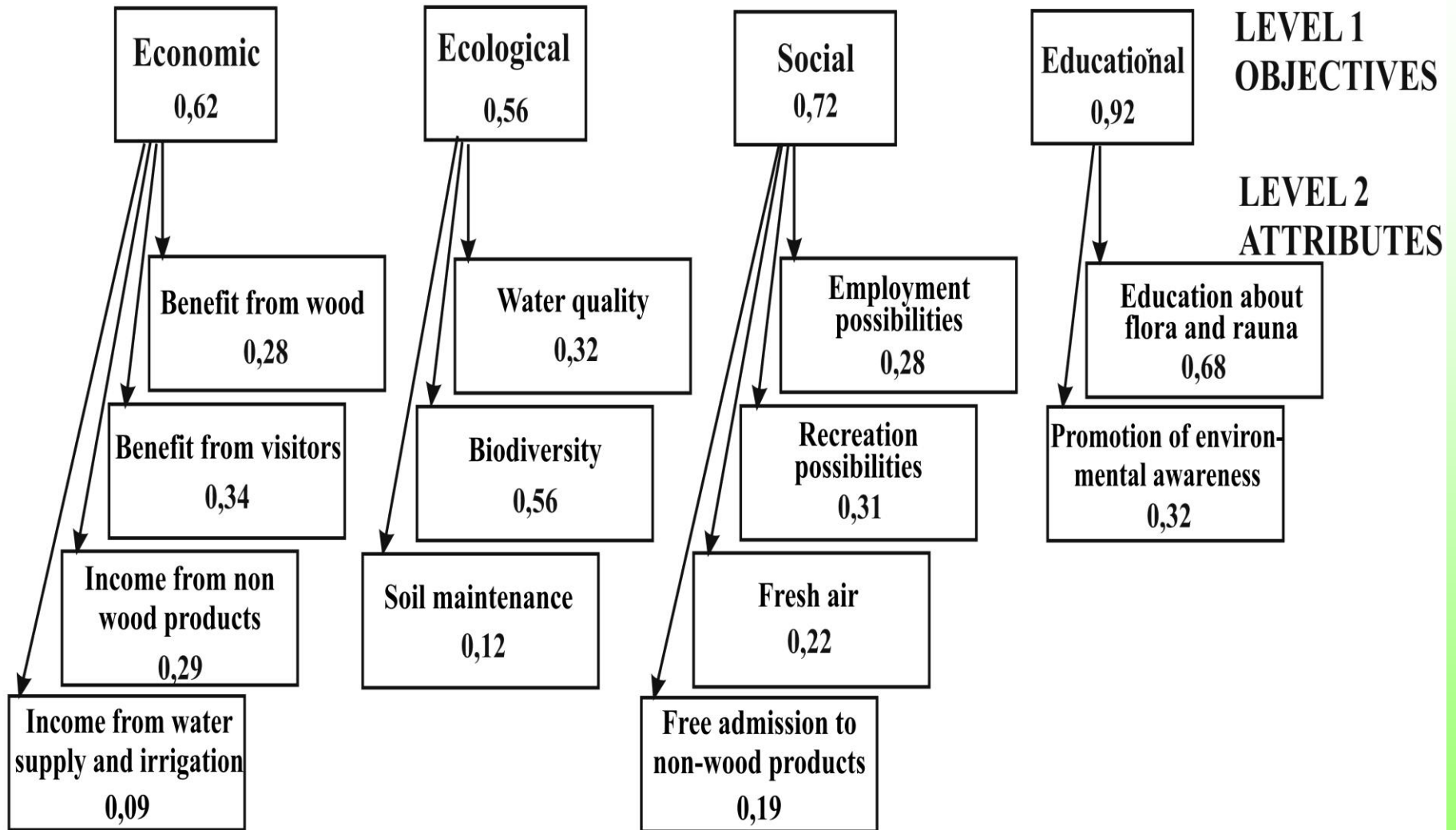
increase and conservation of biodiversity, forest health, increase of quality and quantity of water, improvement of fauna and flora, prevention of flood danger, prevention of soil erosion, climate changes, reforestation with autochthonic species, global carbon cycle

Social

free access to nontimber products, recreation, source of wealth for local population, free entrance, employment possibilities

Educational

forest learning trails, preservation of natural heritage, guided tours



Multiple criteria group decision making

- Forest management decisions are made under a multiple decision maker context.
- Many stakeholders, owners, forest managers, ecologists, and public participate in forest resource use and conservation; they promote communication between the interest groups
- The decision maker gathers the information about the values, attitudes and beliefs of the interest groups.

Multiple-criteria and group decision making models – a theoretical approach

- **Multiple-criteria models (MCM)** and methods imply a process of assigning values to alternatives that are evaluated along multiple-criteria.
- MCM deal with the selection of the best alternative based on conflicting objectives.
- MCM vary across decision making problems (GP, MAUT, SMART, ELECTRE, AHP, ANP,.....).
- The problems present a challenge for developing new multiple-criteria methodologies.

- MCM problems can be single-decision maker problems or group decision problems (GDP).
- GDP techniques provide a framework to represent the decision groups into a single model and are searching for group valuation of alternatives:
 - compromise
 - voting
 - consensus
 - aggregating methods
 - the aggregation of individual priorities
 - the aggregation of individual judgments

AHP and group methods

- According to hierarchical structure of a FM problem we are favoring AHP.
- AHP is rated very high compared with other MCM regarding applicability, validity of outcomes, structure, etc. (Peniwati, 2007)
- AHP, with its modified form ANP, was developed by Saaty in 1980, first for one decision maker.
- Eigenvector method: $Aw = \lambda_{\max} \cdot w$

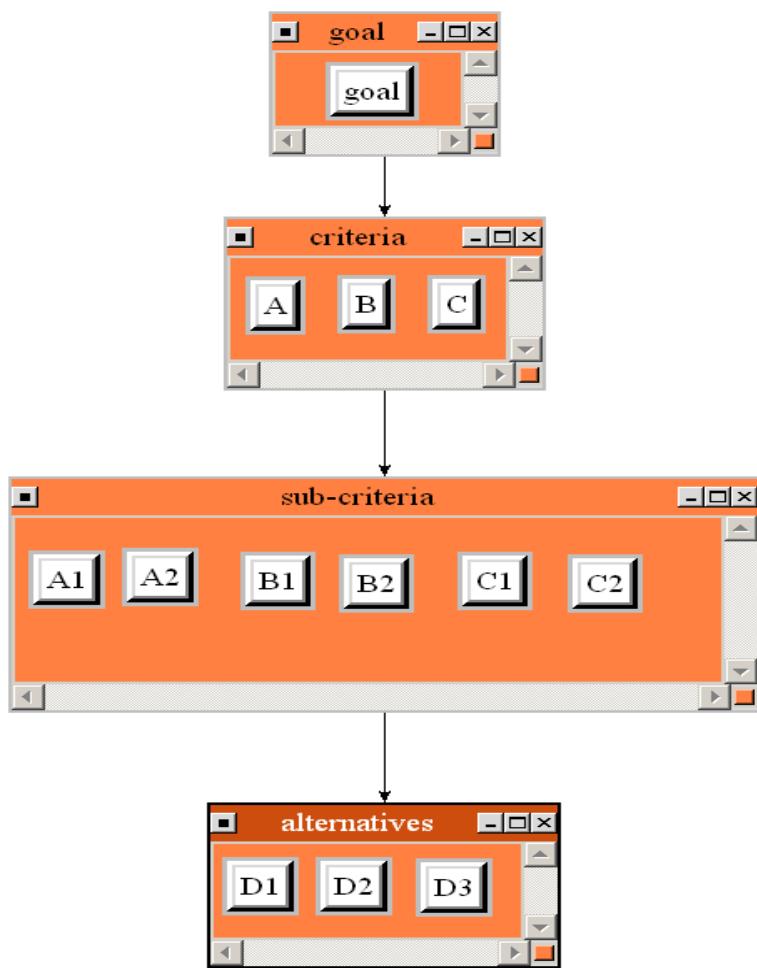
Comparison matrices of three decision makers for economic, ecological, educational and social criteria and their priority vectors

$$A = \begin{bmatrix} 1 & 3 & 2 & \frac{1}{2} \\ \frac{1}{3} & 1 & \frac{1}{5} & \frac{1}{5} \\ \frac{1}{2} & 5 & 1 & 1 \\ 2 & 5 & 1 & 1 \end{bmatrix} \quad w_A = \begin{bmatrix} 0.2897 \\ 0.0698 \\ 0.2688 \\ 0.3718 \end{bmatrix}$$

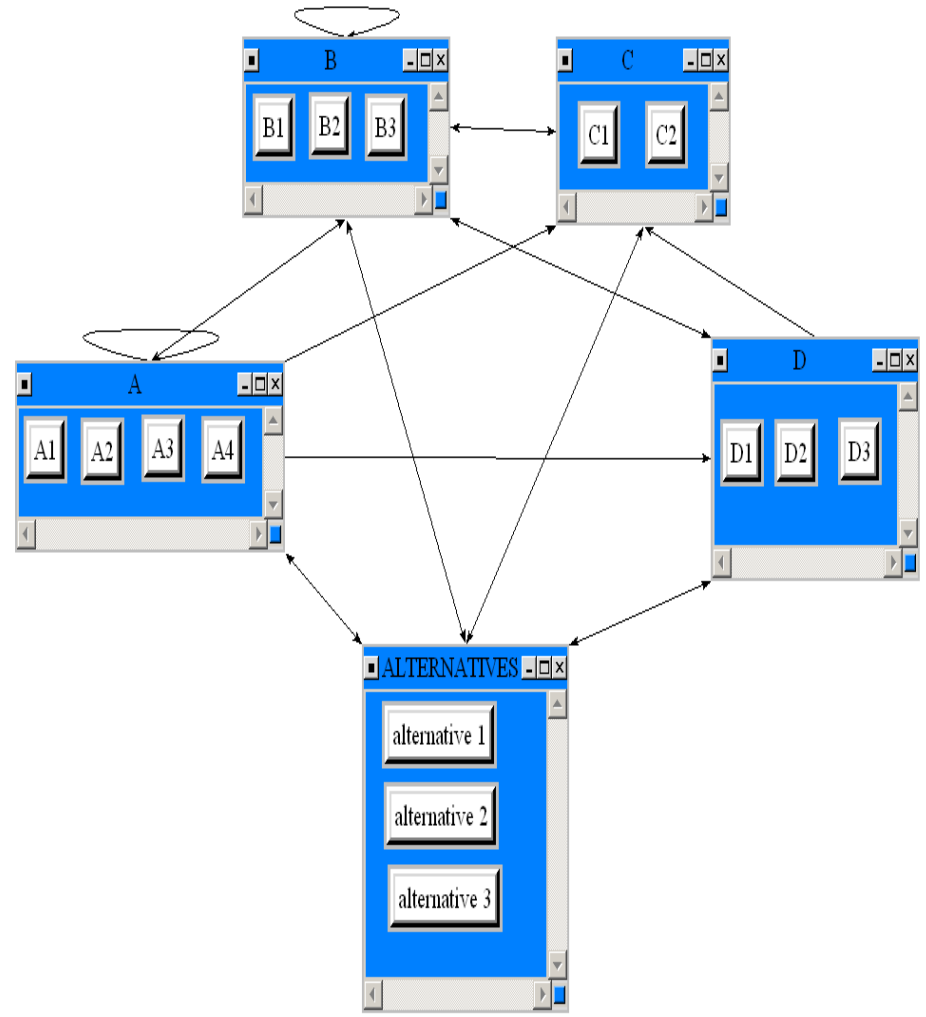
$$C = \begin{bmatrix} 1 & \frac{1}{2} & 4 & 1 \\ 2 & 1 & 6 & 5 \\ \frac{1}{4} & \frac{1}{6} & 1 & \frac{1}{5} \\ 1 & \frac{1}{5} & 5 & 1 \end{bmatrix} \quad w_C = \begin{bmatrix} 0.2149 \\ 0.5384 \\ 0.0568 \\ 0.1899 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & \frac{1}{2} & \frac{1}{2} & 1 \\ 2 & 1 & 3 & 3 \\ 2 & \frac{1}{3} & 1 & 3 \\ 1 & \frac{1}{3} & \frac{1}{3} & 1 \end{bmatrix} \quad w_B = \begin{bmatrix} 0.1529 \\ 0.4611 \\ 0.2620 \\ 0.1241 \end{bmatrix}$$

Super-Decisions; AHP



Super-Decisions; ANP



New multiple criteria group approaches

- Weighted geometric mean method - WGMM (Saaty, 1980, Aczel and Saaty, 1983))
- Aggregation of individual preference structures (Escobar and Moreno-Jimenez, 2007)
- Taguchi's loss function (Cho and Cho, 2008)
- Goal programming (Bryson and Joseph, 1999)
- Fuzzy preference programming (Mikhailov, 2004)
- Weighted least squares group method (Sun and Greenberg, 2006)
- DEA group method (Wang and Chin, 2009)
- Weighted geometric mean method within DEA – WGMDEA (Grošelj, Zadnik Stirn, 2009)

Weighted geometric mean method - WGMM (Saaty)

In the group decision making there are m decision makers with $n \times n$ comparison matrices $A^{(k)} = (a_{ij}^{(k)})$, $k=1, \dots, m$. The importance of k -th decision maker's opinion is denoted by α_k . In the WGMM, their group opinion is presented by the weighted geometric mean complex judgment

matrix $A^{WGM} = (a_{ij}^{WGM})_{n \times n}$

where $a_{ij}^{WGM} = \prod_{k=1}^m (a_{ij}^{(k)})^{\alpha_k}$

The group priority vector from A^{WGM} is then derived by the eigenvector method.

Weighted least squares group method (Sun and Greenberg)

$$\begin{aligned} \min \quad f(\mathbf{w}) &= \sum_{k=1}^m \alpha_k \sum_{j=1}^n \sum_{i=1}^n \left\| a_{ij}^{(k)} w_j - w_i \right\|_2 \\ &= \sum_{k=1}^m \sum_{j=1}^n \sum_{i=1}^n \alpha_k \left(a_{ij}^{(k)} w_j - w_i \right)^2 \end{aligned}$$

$$\begin{aligned} \text{subject to} \quad & \sum_{i=1}^n w_i = 1, \\ & w_i > 0, \quad i=1, \dots, n \end{aligned}$$

The solution of the weighted least squares group method

$$\text{Let } \tilde{A} = \begin{pmatrix} \tilde{a}_{ij} \end{pmatrix}_{n \times n}, \quad \tilde{a}_{ij} = \sum_{k=1}^m \alpha_k a_{ij}^{(k)},$$

$$\hat{a}_{ij} = \sum_{k=1}^m \alpha_k \left(a_{ij}^{(k)2} + 1 \right), \quad \eta_j = \sum_{i=1}^n \hat{a}_{ij} \quad \text{and} \quad \Lambda = \text{diag} \left(\eta_1, \eta_2, \dots, \eta_n \right)$$

Then the group priority vector is given by $w = C^{-1} \lambda$,

$$\text{where } C = \tilde{A} + \tilde{A}^T - \Lambda, \quad C^{-1} = \begin{pmatrix} c_{ij} \end{pmatrix}_{n \times n}$$

$$\text{and } \lambda = \left(\frac{\bar{\lambda}}{2}, \frac{\bar{\lambda}}{2}, \dots, \frac{\bar{\lambda}}{2} \right)^T, \quad \bar{\lambda} = 2 / \left(\sum_{i=1}^n \sum_{j=1}^n \bar{c}_{ij} \right).$$

DEA group method (Wang and Chin)

n criteria, m decision makers with comparison matrices $A^{(k)} = (a_{ij}^{(k)})_{n \times n}$, $k=1, \dots, m$, $\sum_{k=1}^m \alpha_k = 1$

LP model:

$$\max w_0 = \sum_{j=1}^n \left(\sum_{k=1}^m \alpha_k a_{0j} \right) x_j,$$

$$\text{subject to } \sum_{j=1}^n \left(\sum_{k=1}^m \sum_{i=1}^n \alpha_k a_{ij} \right) x_j = 1,$$

$$\sum_{j=1}^n \left(\sum_{k=1}^m \alpha_k a_{ij} \right) x_j \geq nx_i, \quad i = 1, \dots, n$$

$$x_j \geq 0, \quad j = 1, \dots, n$$

WGMDEA (Grošelj, Zadnik Stirn)

It uses the weighted geometric mean that keeps the reciprocal property.

LP model:

$$\max \quad w_0 = \sum_{j=1}^n \left(\prod_{k=1}^m \left(\frac{v_{0j}^{(k)}}{\alpha_k} \right)^{\alpha_k} \right) x_j$$

$$\text{subject to:} \quad \sum_{j=1}^n \left(\sum_{i=1}^n \prod_{k=1}^m \left(\frac{v_{ij}^{(k)}}{\alpha_k} \right)^{\alpha_k} \right) x_j = 1$$

The numerical example:

$$A = \begin{bmatrix} 1 & 3 & 2 & \frac{1}{2} \\ \frac{1}{3} & 1 & \frac{1}{5} & \frac{1}{5} \\ \frac{1}{2} & 5 & 1 & 1 \\ 2 & 5 & 1 & 1 \end{bmatrix}$$

$$CR_A = 0.0824$$

$$\alpha_A = 0.5$$

$$B = \begin{bmatrix} 1 & \frac{1}{2} & \frac{1}{2} & 1 \\ 2 & 1 & 3 & 3 \\ 2 & \frac{1}{3} & 1 & 3 \\ 1 & \frac{1}{3} & \frac{1}{3} & 1 \end{bmatrix}$$

$$CR_B = 0.0656$$

$$\alpha_B = 0.25$$

$$C = \begin{bmatrix} 1 & \frac{1}{2} & 4 & 1 \\ 2 & 1 & 6 & 5 \\ \frac{1}{4} & \frac{1}{6} & 1 & \frac{1}{5} \\ 1 & \frac{1}{5} & 5 & 1 \end{bmatrix}$$

$$CR_C = 0.0728$$

$$\alpha_C = 0.25$$

Results

	WGMM	Rank	WLSGM	Rank	Group DEA	Rank	WGMDEA	Rank
economic	0.2741	2	0.3970	1	0.2150	4	0.2724	2
ecological	0.2214	3	0.1583	4	0.2788	1	0.2253	3
educational	0.2153	4	0.1726	3	0.2409	3	0.2259	4
social	0.2892	1	0.2721	2	0.2653	2	0.2764	1

- The example given here as well as others (Grošelj, Zadnik Stirn, 2009-EJOR, CEJOR) show the differences in results.
- Some methods have drawbacks (violation of reciprocal property, etc.)
- WGMM and WGMDEA give similar results.
- The advantage of WGMDEA is LP (WGMM uses eigenvector procedure).

Conclusions

- In the presentation the central concern of solving a sophisticated FM problem is an integrated approach to MCDA methodologies.
- We discussed the idea of drawing together different MCDA methodologies to provide a meta-solution to multi-criteria and group FM problem
- Such considerations lead to the research needs in the area of MCDA.

Some references:

- KEENLY, R.L. and RAIFFA, H., 1976, *Decision with multiple objectives: preferences and value trade-offs*. John Wiley, New York.
- BELTON, V. and STEWART, T.J., 2002, *Multiple criteria decision analysis*. Kluwer, Dordrecht, NL.
- SAATY, T.L., 1980, *The Analytic Hierarchy Process: Planning, Priority Setting, Resource Allocation*, McGraw-Hill, New York.
- ACZEL, J., SAATY, T., 1983, Procedures for synthesis of judgments. *Journal of Mathematical Psychology*, 1983/27: 93-102.
- CHANG, S. and BUONGIORNO, J., 1981, A programming for multiple use forestry. *J. of Env. Manage.*, 13: 45-58.
- DIAZ-BALTEIRO, L. and ROMERO, C., 1998, Modelling timber harvest scheduling problems with multiple criteria: an application to Spain, *Forest Science*, 44: 47-57.
- SHIELDS, D.J., TOLWINSKI, B., KENT, B.M., 1999. Models for conflict resolution in ecosystem management. *Socio-economic planning sciences* 33: 61-84.
- MENDOZA, G.A. and PRABHU, R., 2003, Qualitative multi-criteria approaches to assessing indicators of sustainable forest resource management, *For. Ecol. and Manage.*, 174: 329-343.
- PHUA, M. and MINOWA, M., 2004, A GIS-based multicriteria decision making approach to forest conservation planning at a landscape scale: a case study in the Kinabalu Area, Sabah, Malaysia, *Landscape and Urban Planning*, 71:207-222.
- ZADNIK STIRN, L., 2006, Integrating the fuzzy analytic hierarchy process with dynamic programming approach for determining the optimal forest management decisions. *Ecol. model.*, 194/1: 296-305.
- ZADNIK STIRN, L. 2009, Analyzing forest management alternatives within interdependent goals. In *Building insights of managerial economics and accounting towards sustainable forest management: Proceedings of the IUFRO unit 4.05.00 international symposium. May 17-19, 2007, Lviv, Ukraine. Edited by L. Zahvoyska, H. Joebstl, S. Kant, L. Maksymiv. UNFU Press, Kamula, Lviv, Ukraine.*
- GROŠELJ, P. and ZADNIK STIRN, L., 2009, Comparison of group methods in AHP. *Proceedings of the 10th Int. symposium on OR*, Nova Gorica, Slovenia, Sept. 23-25, 2009, pp. 157-163.
- GROŠELJ, P. and ZADNIK STIRN, L., 2009, Acceptable consistency of aggregated comparison matrices in AHP, submitted to EJOR
- GROŠELJ, P. and ZADNIK STIRN, L., 2009, Methods based on data envelopment analysis for deriving²³ group priorities in AHP; submitted to CEJOR.